

week7

Tommy
MacWilliam

pset4

Valgrind

Bitwise
Operators

Linked Lists

Stacks/Queues

Hashtables

Binary Trees

Tries

Practice
Problems

week7

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Announcements

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Problems

- ▶ pset4: returned
- ▶ pset5 scavenger hunt!
 - ▶ submit sooner in the event of a tie!
- ▶ pset6 challenge!

Today

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Practice
Problems

- ▶ pset4
- ▶ Valgrind
- ▶ Bitwise Operators
- ▶ Linked Lists
- ▶ Stacks/Queues
- ▶ Hash Tables
- ▶ Binary Search Trees
- ▶ Tries

#1 Design Mistake

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Problems

- ▶ don't run an expensive function unless you have to!
- ▶ remember `strlen()`? we moved that outside of loops because we didn't need to rerun an expensive function every loop iteration
 - ▶ if we're not modifying a string, its length will never change, so we don't need to recalculate it

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Problems

- ▶ in Sudoku, won() is an expensive function
- ▶ many moves (e.g. move cursor, delete number) will not alter whether or not the board is won or not
 - ▶ so, we shouldn't be recalculating won()
- ▶ solution: cache the result of won in a variable
 - ▶ checking the value of a variable is much faster than running won()

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Problems

- ▶ in fact, caching is a popular programming technique
- ▶ in many cases, perfectly-up-to-date data is unnecessary
 - ▶ for example, Facebook caches the number of friends you have
 - ▶ recalculating the friend count every time someone views your page is unnecessary, since that won't get you any more friends

Valgrind

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Problems

- ▶ another debugging tool (just like GDB)!
- ▶ GDB helps us find segfaults and logic errors, while Valgrind finds memory errors
- ▶ To run: `valgrind -v --leak-check=full ./<program>`

Valgrind

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Problems

▶ example time!

▶ `helpmevalgrind.c`, `valgrindsavestheday.c`

Bitwise Operators

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Problems

- ▶ allow operations in the individual bits of a variable
- ▶ `&` - bitwise and
- ▶ `|` - bitwise or
- ▶ `^` - bitwise exclusive or (XOR)
- ▶ `<<` - left shift
- ▶ `>>` - right shift
- ▶ `~` - not

Bitwise Operators

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Operators**

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Practice
Problems

▶ $0 \ \& \ 0 = 0$

▶ $0 \ \& \ 1 = 0$

▶ $1 \ \& \ 0 = 0$

▶ $1 \ \& \ 1 = 1$

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Problems

▶ $0 \mid 0 = 0$

▶ $0 \mid 1 = 1$

▶ $1 \mid 0 = 1$

▶ $1 \mid 1 = 1$

Bitwise Operators

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Problems

▶ $0 \wedge 0 = 0$

▶ $0 \wedge 1 = 1$

▶ $1 \wedge 0 = 1$

▶ $1 \wedge 1 = 0$

Bitwise Operators

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Problems

► $2 \ \& \ 3 = 0010 \ \& \ 0011 = 0010 = 2$

► $13 \ | \ 4 = 1101 \ | \ 0010 = 1111 = 15$

► $7 \ ^ \ 3 = 0111 \ ^ \ 0011 = 0100 = 4$

Bitwise Operators

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Problems

- ▶ swapping numbers like a hacker with XOR

```
void swap(int* a, int* b) {  
    a ^= b; b ^= a; a ^= b;  
}
```

- ▶ `int a = 3, b = 4; swap(&a, &b);`
 - ▶ `a ^= b:` `a = 0011 ^ 0100 = 0111;`
 - ▶ `b ^= a:` `b = 0100 ^ 0111 = 0011;`
 - ▶ `a ^= b:` `a = 0111 ^ 0011 = 0100;`
 - ▶ **now** `a = 4, b = 3`
- ▶ **caveat:** only works when `a != b`

Bitwise Operators

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Problems

- ▶ $5 \ll 2 = 00000101 \ll 2 = 00010100 = 20$
- ▶ $15 \gg 2 = 00001111 \gg 2 = 00000011 = 3$
- ▶ $\sim 13 = \sim 1101 = 0010 = 2$

Linked Lists

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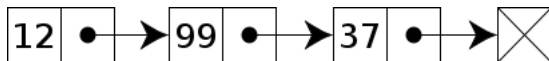
Stacks/Queues

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Practice
Problems



- ▶ each node contains a value and a pointer to the next node
 - ▶ need to maintain a pointer to the first node
 - ▶ last node points to `NULL`

Traversing

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Practice
Problems

- ▶ create pointer to iterate through list, starting at first element
- ▶ loop until iterator is `NULL` (aka no more elements)
- ▶ at every point in loop, iterator will point at an element in the linked list
 - ▶ can access any element of the element
- ▶ to go to next element, simply move iterator to `next`

Traversing

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Practice
Problems

```
node* iterator = first;
while (iterator != NULL)
{
    printf("%s\n", iterator->word);
    iterator = iterator->next;
}
```

Inserting at Head

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Practice
Problems

- ▶ make new node point to previous first node
- ▶ make root point to new node

Inserting at Head

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Problems

```
node_to_insert->next = first;  
root->next = node_to_insert;
```

Inserting at Tail

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Practice
Problems

- ▶ make last node point to new node
- ▶ make new node point to `NULL`

Inserting at Tail

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Problems

```
last->next = node_to_insert;  
node_to_insert->next = NULL;
```

Deleting

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Practice
Problems

- ▶ make previous node point to next node
- ▶ free node

Deleting

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Problems

```
previous_node->next = node_to_remove->next;  
free(node_to_remove);
```


Linked Lists

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Practice
Problems

▶ example time!

▶ `list.c`

Stacks/Queues

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Practice
Problems

- ▶ a linked list is one type of data structure
 - ▶ data structure is a general term referring to how to store multiple complex datatypes (like structs) in memory
 - ▶ data structures can be more than just linear lists, as we'll soon see
- ▶ stacks and queues can be specific types of linked lists
 - ▶ answer the questions: where do I put new elements in the list? which element is the “first” element?

Stacks

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Practice
Problems

- ▶ LIFO: last in, first out
- ▶ put new element at end of list, take element off end of list
- ▶ example: the stack in memory
 - ▶ put new stack frame on top, remove stack frame from top when done

Queues

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Tries

Practice
Problems

- ▶ FIFO: first in, first out
- ▶ put new element at end of list, take element off beginning of list
- ▶ example: networks
 - ▶ handle requests in the order they come in

Stacks/Queues

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Practice
Problems

- ▶ how can we use our linked list implementation from last week to implement both stacks and queues?
- ▶ stack: insert new element at end using `insert_tail`, then look at last element of the list
 - ▶ or, insert new element at beginning using `insert_head`, then look at first element of list
- ▶ queue: insert new element at beginning using `insert_head`, then look at last element of list
 - ▶ or, insert new element at end using `insert_tail`, then look at first element of list

Hashtables

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Practice
Problems

- ▶ also known as a hashmap, unordered map, etc.
- ▶ like an array: each “key” corresponds to a numerical position in the hashtable
 - ▶ keys don’t have to be numbers (string keys can be very helpful)
- ▶ keys are “mapped” to values via a hash function
 - ▶ example hash function: sum the letters of a string
 - ▶ “hello” maps to position $104 + 101 + 108 + 108 + 111 = 532$

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Problems

- ▶ problem: what if a value maps to a key larger than our hashtable?
 - ▶ solution: use mod to ensure no key is greater than hashtable size
- ▶ problem: what if two values map to the same key?
 - ▶ solution: each element of the hashtable is a linked list to values that hash to that value (separate chaining)
 - ▶ solution: store the value at another location in the hashtable (probing)
 - ▶ many other solutions!

Hashtables

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Practice
Problems

- ▶ insertion/lookup just like an array
 - ▶ calculate hash of key, then use that just like an array index
 - ▶ both $O(1)$, very fast
- ▶ however, have to consider:
 - ▶ time it takes to hash a value
 - ▶ length of time it takes to resolve a collision

Hashtables

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Practice
Problems

- ▶ example time!
 - ▶ `hashtable.c`

Binary Trees

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Practice
Problems

- ▶ like a linked list, but nodes arranged in a tree rather than in a straight line
- ▶ each node has at most two child nodes (contrast with the linked list, where each node has one child node)
 - ▶ value of left child node must be less than value of parent node
 - ▶ value of right child node must be greater than value of parent node

Binary Trees

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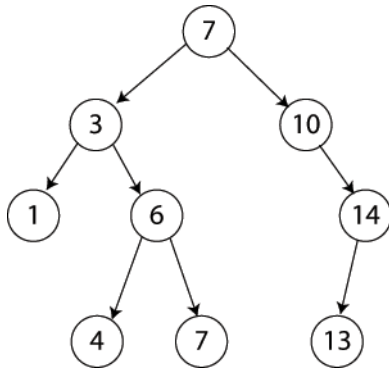
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Binary Trees

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Problems

► insertion

- start at root node
- compare root value to value to insert
- if less, use the root's left child as the root and repeat
- if greater, use the root's right child as the root and repeat
- if the appropriate child is null, then insert new value

Binary Trees

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Problems

► search

- compare value to root node
- if less, use root's left child as the root and repeat
- if greater, use root's right child as the root and repeat
- if appropriate child is null, then value is not present in the tree

Binary Trees

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Practice
Problems

- ▶ insertion/search: $O(\log n)$
- ▶ just like binary search: cutting the problem in half with each iteration

Binary Trees

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Problems

- ▶ **example time!**
 - ▶ `binarytree.c`

Tries

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Practice
Problems

- ▶ also a tree, but each node can have more than two children
- ▶ in a trie that stores words, each node contains a single letter in a word
 - ▶ each child node of represents the next letter in some word
 - ▶ so each node can have at most 26 children

Tries

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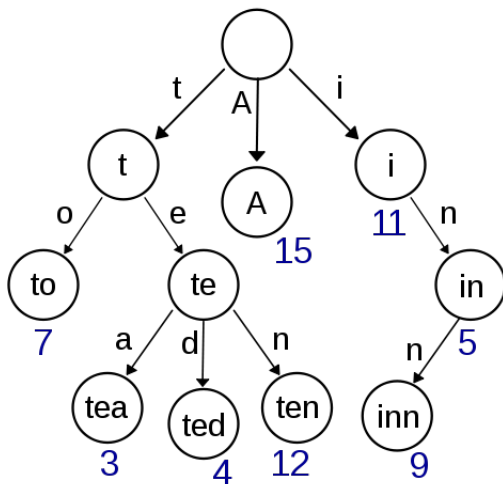
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► insertion

- start with first letter of word to insert
- create root node representing first letter if necessary
- move to next letter of word, using that node as the new root node

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► search

- start with first letter of word to insert
- check if child node of that letter exists
- if so, use that node as the new root node and move on to next letter
- if no child node exists and we have not reached the end of the search word, it isn't found in the trie
- if we reach the end of the search word, it exists in the trie

Practice Problems

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Practice
Problems

- ▶ sum the elements of a binary tree
 - ▶ hint: it's a one-line function!
- ▶ print out the elements of a binary tree from least to greatest
- ▶ set/unset the rightmost bit of an integer